

Image Transforms

unit-II

- * It is extensively used in Image processing and image analysis.
- * Transform is a mathematical tool \Rightarrow Move from one domain to another domain.
- * Reason \rightarrow perform the task at hand in an easier manner.
- * It is useful for fast Computation of convolution and correlation.
- * It change the representation of a signal by projecting it onto a set of basis functions.
- * It do not change the Inf content present in the signal.
- * Most Image transforms give Inf about freq content in image.
- * All the transforms will not give freq domain inf.

* Significant role

①

Image processing apps



Image analysis

Image enhancement

Image filtering

Image Compression.

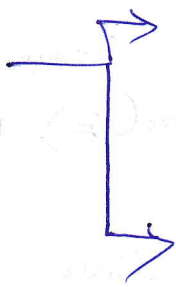
Need for Transform

- 1) Mathematical Convenience.
- 2) Extract more Inf.

Image Transforms

* Basically a representation of an image.

* 2 reasons



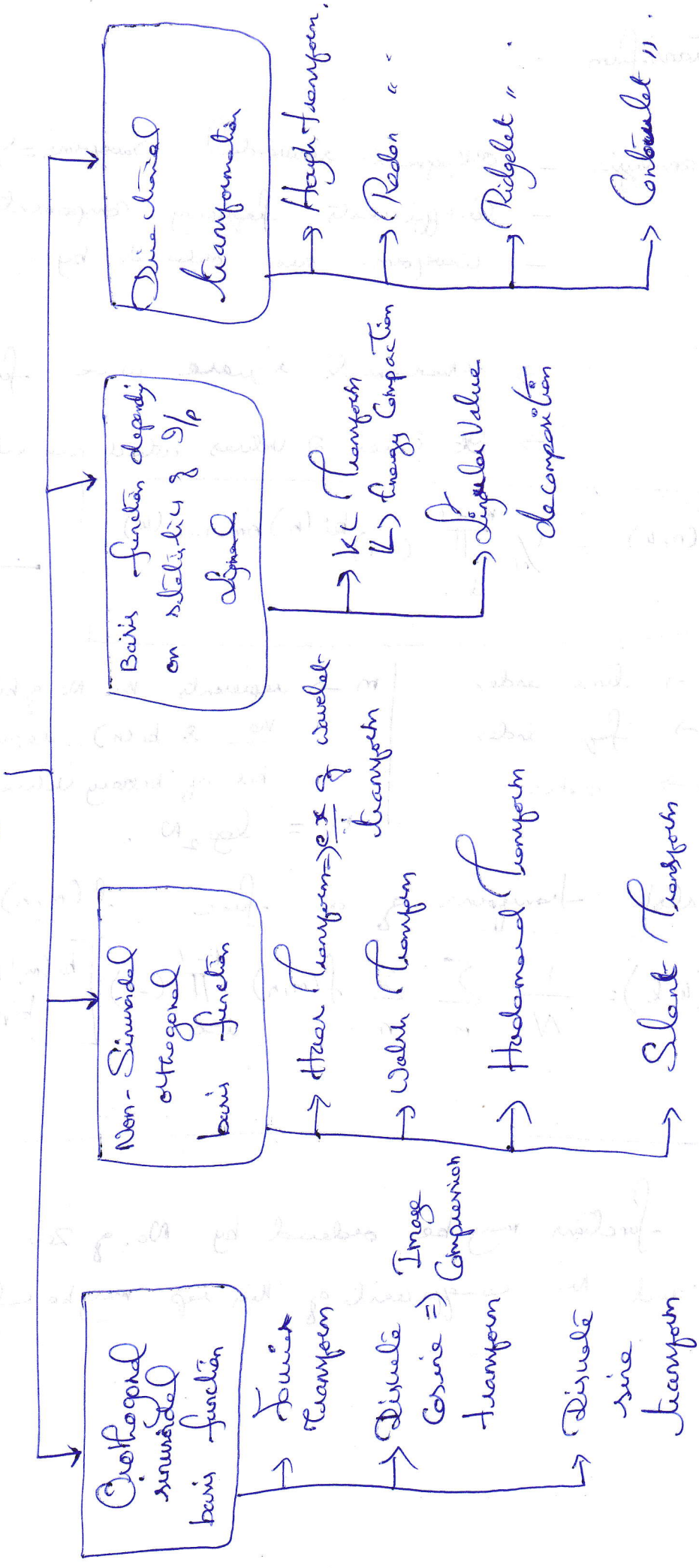
Transformation may isolate critical components of the image pattern so that they are directly accessible analysis.

And the transformation may place the image data in a more compact form so that they can be stored and transmitted efficiently.

Different types of Image Transforms

- 1) Fourier Transform
- 2) Walsh Transform
- 3) Hadamard Transform
- 4) Slant Transform
- 5) Discrete cosine Transform
- 6) K-L Transform
- 7) Radon Transform
- 8) Wavelet Transform

Image Transforms



Orthogonal sinusoidal basis function

Fourier Transform

Discrete Cosine Transform

Discrete Sine Transform

Non-Sinusoidal orthogonal basis function

Haar Transform & wavelet Transform

Walsh Transform

Hadamard Transform

Slant Transform

Basis function depends on statistics of signal

K-L Transform

Energy Compaction

Singular Value decomposition

Discrete Transformation

High Transform

Radon Transform

Ridgelet Transform

Contourlet Transform

Walsh Transform

- Fourier analysis - orthogonal sinusoidal waveforms \Rightarrow Represented
- Coefficients frequency components
 - Waveforms are ordered by freq.

Walsh

- \rightarrow orthogonal square wave functions
- \rightarrow It takes 2 values which are either $+1$ or -1

$$g(n, k) = \frac{1}{N} \prod_{i=0}^{m-1} (-1)^{b_i(n) b_{m-1-i}(k)}$$

Here $n \rightarrow$ time index
 $k \rightarrow$ freq index
 $N \rightarrow$ order

$m \rightarrow$ represents the No. of bits to represent a
no. & $b_i(n)$ represents i^{th} (from
left) bit of binary value.
 $m = \log_2 N$.

2D Walsh Transform of a func $f(m, n)$ is given by

$$F(k, l) = \frac{1}{N} \sum_m \sum_n f(m, n) \prod_{i=0}^{p-1} (-1)^{b_i(m) b_{p-1-i}(k) + b_i(n) b_{p-1-i}(l)}$$

Sequence

Walsh functions may be ordered by No. of zero crossings or
frequency and the coefficients of this rep may be called seq
components.

Slant Transform

- * It is an orthogonal transform \Rightarrow Sawtooth waveform (or) Slant basis vectors.
- * Slant basis vector is monotonically \downarrow in constant steps from max to min has separability property & has fast Computational Algorithm.
- * \rightarrow It reproduces linear variations of brightness
- \rightarrow Its performance at edges is not as optimal as the DCT.
- \rightarrow \therefore Slant nature of lower order coefficients its effect is to smoothen the edges.