

DPCM.

- * If a voice (or) video signal is sampled at a rate slightly higher than the Nyquist rate, then the resulting sampled signal is found to be exhibit a high correlation between adjacent samples \Rightarrow This high correlation is that in an average sense, the signal does not change rapidly from one sample to the next.
- * When these highly correlated samples are encoded as in a std PCM systems, the resulting encoded signal contains redundant information.
- * Now it is clear that symbols that are not absolutely essential to the T_x of Inf are generated as a result of the encoding process.

Prediction:

Knowing the past behaviour of a signal up to a certain point in time, it is possible to make some inference about its future values, \Rightarrow Such a process is commonly called Prediction.

Delta modulation :-

PCM & DPCM \Rightarrow

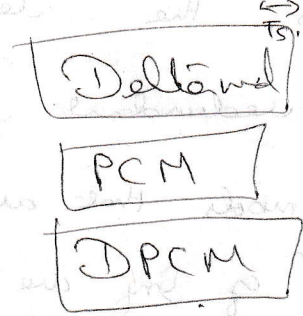
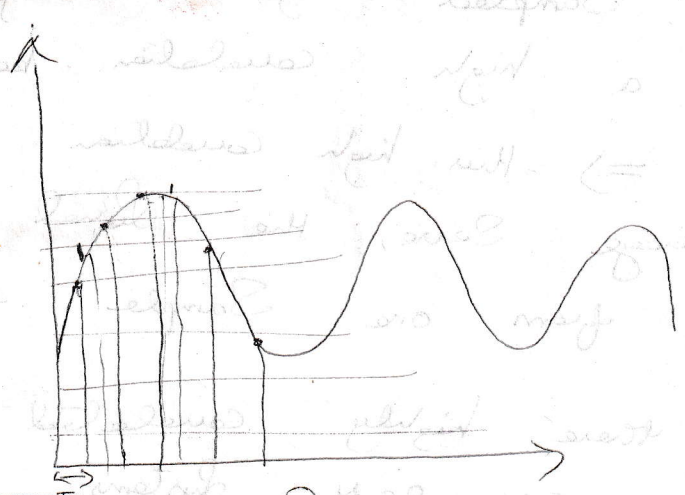
$$f_s \geq 2 \omega$$

Sampling rate $>$ Nyquist rate

Delta modulation

DPCM

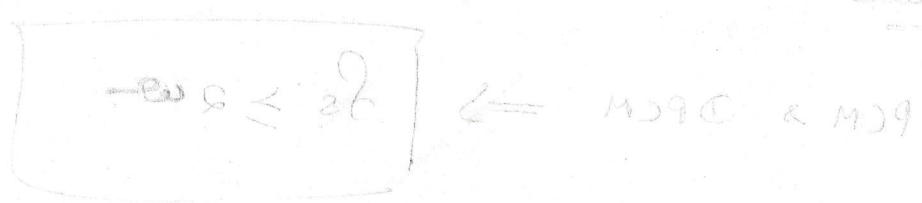
Asymmetrical \Rightarrow Non PCM & DPCM



bit rate reduction

Delta

Asymmetrical \Rightarrow Non PCM & DPCM



Asymmetrical \Rightarrow Non PCM & DPCM

$$H = \begin{bmatrix} y_4 & y_2 & y_4 \\ y_2 & 1 & y_2 \\ y_4 & y_2 & y_4 \end{bmatrix} \Rightarrow 2 \cdot \frac{3}{4} + 1 \cdot \frac{1}{4} = 4$$

Scaling is 4 \Rightarrow center pol is 1.

$$\begin{bmatrix} 1 & 0 & 7 & 0 \\ 0 & 0 & 0 & 0 \\ 3 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} \quad 4 \cdot \begin{bmatrix} y_4 & y_2 & y_4 & 0 \\ y_2 & 1 & y_2 & 0 \\ y_4 & y_2 & y_4 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 7 & 0 \\ \vdots & \vdots & \vdots & \vdots \\ \vdots & \vdots & \vdots & \vdots \\ \vdots & \vdots & \vdots & \vdots \end{bmatrix}$$

$$A_1 = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix} \quad A_2 = \begin{bmatrix} \sqrt{2} & j \\ -j & \sqrt{2} \end{bmatrix}$$

orthogonal $\Rightarrow A^{-1} = A^T \Rightarrow A^{-1}A^T = I$

$$A_1^T = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix} \quad |A_1| = \frac{1}{\sqrt{2}} (-2) = \frac{-\sqrt{2} \cdot \sqrt{2}}{\sqrt{2}} = -\sqrt{2}$$

$$A_1^{-1} = \frac{1}{|A_1|} [\text{adj } A_1] = \frac{1}{(-\sqrt{2})} \begin{bmatrix} -1 & -1 \\ -1 & 1 \end{bmatrix}$$

$$= \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$$

$\therefore A^{-1} = A^T$ hence it is orthogonal.

$$A_2 = \begin{bmatrix} \sqrt{2} & j \\ -j & \sqrt{2} \end{bmatrix}$$

$$|A_2| = 2 + j$$

$$A_2^T = \begin{bmatrix} \sqrt{2} & -j \\ j & \sqrt{2} \end{bmatrix}$$

$$A_2^{-1} = \frac{1}{(A_2)} [\text{adj } A_2] = \frac{1}{2+j} \begin{bmatrix} \sqrt{2} & +j \\ -j & \sqrt{2} \end{bmatrix}$$

$$A^{-1} = A^{*T}$$

$$A_2^{*T} = \begin{bmatrix} \sqrt{2} & j \\ -j & \sqrt{2} \end{bmatrix}$$

$$= \frac{1}{2+j}$$

2

$$\begin{array}{|c|cc} \hline 1 & 4 & 1 \\ \hline 2 & 5 & 3 \\ \hline \end{array} \Rightarrow \begin{bmatrix} 1 & 2 \\ 4 & 5 \\ 1 & 3 \end{bmatrix}$$

$M_1 \times N_1$
 3×2

$$\begin{aligned} & (M_1 + M_2 - 1) \times (N_1 + N_2 - 1) \\ & (3 + 2 - 1) \times (2 + 2 - 1) \\ & (5 - 1) \times (4 - 1) \end{aligned}$$

$$\begin{array}{|c|c} \hline 1 & 1 \\ \hline 1 & -1 \\ \hline \end{array} \Rightarrow \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$$

$M_2 \times N_2$
 2×2

4×3

$$\begin{array}{|c|ccc} \hline 1 & 1 & 1 & \\ \hline 4 & 4 & 4 & \\ \hline 1 & 1 & 1 & \\ \hline \end{array} \Rightarrow$$

$$\begin{bmatrix} 1 & 5 & 5 & 1 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$\begin{array}{|c|cc} \hline 1 & -1 & \\ \hline 4 & 4 & -4 \\ \hline 1 & 1 & -1 \\ \hline \end{array} \Rightarrow$$

$$\begin{pmatrix} 1 & 3 & -3 & -1 & 7 \\ 2 & 7 & 8 & 8 & \end{pmatrix}$$

$$\begin{array}{|c|ccc} \hline 1 & 5 & 5 & 1 \\ \hline 3 & 10 & 5 & 7 \\ \hline 2 & 3 & -2 & -3 \\ \hline \end{array}$$

$y(\text{min})$

$$\begin{array}{|c|cc} \hline 1 & 1 & \\ \hline 2 & 2 & 2 \\ \hline 5 & 5 & 5 \\ \hline 3 & 3 & 3 \\ \hline \end{array} \Rightarrow$$

$$2 \quad 3 \quad -2 \quad -3$$

$$\begin{array}{|c|cc} \hline 1 & 1 & \\ \hline 2 & 2 & -2 \\ \hline 5 & 5 & -5 \\ \hline 3 & 3 & -3 \\ \hline \end{array} \Rightarrow$$

